

Optimal Channel Access Schemes for Wireless LAN under Asynchronous Multiple-Packet Reception (MPR)



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Research Background

| | <i>p</i> -Persistent CSMA | | A user begins a packet transmission with a common probability p when it has sensed channel idle, and continues sensing when it has sensed channel busy | | | | | |
|-------------|--|---|--|-----------|---|--------|--|--|
| | Multiple-Pac Reception | ket Suce at the | Multiple-packet reception (MPR) techniques enable successful receptions of time-overlapping packets at the physical layer. | | | | | |
| A pa hea | User Idle / sens probated arrives the ad of the queue | Continue ing with bility 1 - p Continue sensing | Idle / Begin a packet transmission with probability <i>p</i> | Time Axis | User 1 User 2 · · · · · · · | ceiver | | |
| | Figure 1. | <i>p</i> -persistent C | CSMA | | Figure 2. MPR techniques | | | |

Research Background

| Traditional <i>p</i> - single-pac | persistent CSMA under ket reception (SPR) | Traditional <i>p</i> -persistent CSMA under multiple-packet reception (MPR) | | |
|--------------------------------------|--|---|--|--|
| | | | | |
| Limitation 1 | Early studies on <i>p</i> -persis which did not consider t | tent CSMA assumed the SPR model, ne advance of MPR techniques | | |
| Limitation 2 | Further studies on <i>p</i> -personder the synchronous mathematical synchrono | istent CSMA assumed the MPR model node, which led to bandwidth waste | | |
| Limitation 3 | Although some early studo not provide a general access probabilities are | dies have improved the protocol, they analytical model, and the setting of far from the optimum | | |



| Carrier Sensing | We assume that all users can perform carrier sensing to detect if the number of ongoing transmissions is 0,, γ -1 or $\geq \gamma$, and the time required to do so is negligible |
|----------------------------------|---|
| Channel Assumption | We consider that wireless fading effect is negligible , and channel coding is not used to protect the packets. |
| γ-MPR Capability | We assume that the receiver has the γ -MPR capability, i.e., can recover all <i>n</i> signals simultaneously transmitted in a slot if $1 \le n \le \gamma$, and recover none of them otherwise. |
| Packet Length | We consider that the packet lengths correspond to integer numbers of slots , and follow the geometric distribution with average value $\Lambda > 1$ |

Main Contributions





Remark: The aforementioned system model with $\gamma = 1$ is exactly the model for *p*-persistent CSMA under SPR.



Contrib. 1 Protocol Design The generalized *p*-persistent CSMA for the case of N = 3 and $\gamma = 2$.



- 1. At the beginning of slot 1, user 2 and user 3 detect the number of ongoing transmission is 0; thus they begin transmissions with probability p_0 .
- 2. At the beginning of slot 8, user 1 detects the number of ongoing transmission is 1; thus it begins a transmission with probability p_1 .

Contrib. 2 Protocol Analysis

Provide a general analytical model based on a parameterized MDP

Based on the access probability p_n , we define the parameter vector: $\mathbf{p} \triangleq (p_0, p_1, \dots, p_{\gamma-1})$

| | \downarrow |
|------------------------|--|
| State | The <i>state</i> , denoted by <i>n</i> , is defined as the number of ongoing transmissions in the carrier sensing phase. |
| Action | The <i>action</i> , denoted by <i>a</i> , means that <i>a</i> users begin new transmissions after carrier sensing at state <i>n</i> . |
| Parameterized Policy | The <i>parameterized policy</i> , denoted by $\pi_{n,a}(\mathbf{p})$, is defined as the probability that <i>a</i> out of $N - n$ users begin to transmit at state <i>n</i> . |
| Transition Probability | The <i>transition probability</i> , denoted by $\varphi_{n,n'}(\mathbf{p})$, is defined as the probability that the next state is <i>n</i> ' when the present state is <i>n</i> . |
| Roward State | The <i>state reward</i> , denoted by $r_n(\mathbf{p})$, is defined as the average of total packet lengths of all the successful transmissions at state <i>n</i> . |
| Reward action | The <i>action reward</i> , denoted by $r_{n,a}(\mathbf{p})$, is defined as the reward which is achieved when action <i>a</i> is taken at state <i>n</i> . |

Contrib. 2 Protocol Analysis

Theoretical analysis of the state reward $r_n(\mathbf{p})$

We assume that a given packet is being transmitted in both the present and next slots.

 $\xi_{h,h'}(\mathbf{p})$

The probability that there are h' other ongoing transmissions in the next slot when there have been h other ongoing transmissions in the present slot.

 $g_{m,h_1,h_m}(\mathbf{p})$ The probability that there are h_m other ongoing transmissions in the *m*-th slot of a given transmission, and fewer than γ other ongoing transmissions in each of the first *m*-1 slots of the transmission, provided that there are h_1 other ongoing transmissions in the first slot of the transmission.

 $q_{\lambda,h_1}(\mathbf{p})$

The probability that a λ -slot transmission is successful when there are fewer than γ other ongoing transmissions in each of the λ slots of the transmission

 $r_{n,a}(\mathbf{p}) \longrightarrow r_n(\mathbf{p}) \longrightarrow$ Long-term average reward: $R(\mathbf{p}) \Rightarrow$ Throughput

Definition of the optimization problem

Based on the access probability p_n , we define the parameter vector: $\mathbf{p} \triangleq (p_0, p_1, \dots, p_{\gamma-1})$

$$\mathbf{p} \triangleq \left(p_0, p_1, \dots, p_{\gamma-1} \right) \subset \mathbb{D} \triangleq \mathbb{D}_0 \times \mathbb{D}_1 \times \dots \times \mathbb{D}_{\gamma-1}, \text{ where } \mathbb{D}_0 \in (0,1), \ \mathbb{D}_n \in [0,1) \ (n \ge 1)$$

Throughtput $R(\mathbf{p})$ is a function of the parameter vector $\mathbf{p} \rightarrow \exists \mathbf{p} = \mathbf{p}_{opt} \Rightarrow R = R_{max}$

Define the optimization problem $\mathbf{p}_{opt} = \arg \max_{\mathbf{p} \in \mathbb{D}} R(\mathbf{p}), \ R_{\max} = \max_{\mathbf{p} \in \mathbb{D}} R(\mathbf{p})$

Contrib. 3 Protocol Optimization Difficulties of the optimization problem Search $\mathbb{D} \triangleq \mathbb{D}_0 \times \mathbb{D}_1 \times \cdots \times \mathbb{D}_{\gamma-1} \to \text{Find the optimal } \mathbf{p}$ that maximizes $R(\mathbf{p})$ **Modern Optimization** The algorithms possibly takes a very long time to find the near-Algorithms (such as optimal **p**, and are required to set opportune starting points. **Genetic Algorithm**) The term $q_{\lambda,h1}(\mathbf{p})$ in $r_n(\mathbf{p})$ is obtained recursively and the number **Gradient-Based** of recursive steps increases with the geometrically distributed **Methods** packet length. \rightarrow The term $r_n(\mathbf{p})$ is difficult to be calculated. A policy iteration type algorithm that optimizes a special category of parameterized MDPs

| Two Conditions | 1. 2. | The state space can be partitioned such that the transition probabilities and rewards of all states are affected by a distinct parameter or none of parameters in p . The change of the parameters in p does not affect the conditional probability of the state value, known to be included in a partition. |
|----------------|----------|---|

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Difficulties of the optimization problem

Search $\mathbb{D} \triangleq \mathbb{D}_0 \times \mathbb{D}_1 \times \cdots \times \mathbb{D}_{\gamma-1} \to \text{Find the optimal } \mathbf{p}$ that maximizes $R(\mathbf{p})$

The First Condition of the Policy Iteration

The state space can be partitioned such that the transition probabilities and rewards of all states are affected by a distinct parameter or none of parameters in **p**.

The Researched Parameterized MDP

- 1. The reward $r_0(\mathbf{p})$ is affected by all the parameters in \mathbf{p}
- 2. The reward $r_n(\mathbf{p})$ for $0 < n < \gamma$ is affected by all the parameters in \mathbf{p} except p_0

MDP Modification **Mod. 1**: Modify $r_n(\mathbf{p})$ to $r_n^*(\mathbf{p})$ and establish an upper bound on the throughtput \rightarrow Obtain an important observation \rightarrow **Mod. 2**: Modify $r_n(\mathbf{p})$ to $r_n^{**}(\mathbf{p})$ and propose a heuristic design

Mod. 1: Establish an upper bound on the throughtput



Mod. 1: Solve \mathbf{p}_{upp} by the policy iteration (Algorithm 1)

| 1. Initialization | Choose an arbitrary parameter vector $\mathbf{p}^{(0)} \subset \mathbb{D}$ as the initial value and set $k = 0$. | | | |
|-------------------|---|--|--|--|
| 2. Evaluation | Calculate the relative value $v_n^*(\mathbf{p}^{(k)})$ for each $n \in S$ by Bellman equation. | | | |
| 3. Improvement | For $n = 0, 1,, \gamma - 1$, update the new parameter as: $p_n^{(k+1)} = \arg \max_{p_n \in \mathbb{D}} r_n^*(p_n) + \sum_{n' \in \mathcal{S}} \phi_{n,n'}(p_n) v_{n'}^*(\mathbf{p}^{(k)})$ | | | |
| 4. Stopping Rule | If $\mathbf{p}^{(k+1)} = \mathbf{p}^{(k)}$, set $\mathbf{p}_{upp} = \mathbf{p}^{(k)}$ and stop. Otherwise, set $k = k + 1$ and go to step 2. | | | |



Initialization: We set $p_0^{(k)} = \gamma/N$, and $p_n^{(k)} = 0$ for $1 \le n \le \gamma - 1$.

Conclusion: It can be seen that only **6 iterations** are needed to satisfy the stopping rule.

- Contrib. 3 Protocol Optimization
- Mod 1: Comparisons between the throughput and its upper bound

Remark: We set the maximum number of allowed retransmissions to be infinitely large.



Conclusion: Relative gaps between the throughput performance and its upper bound are significant correlation with the parameter Λ and the parameter γ

Mod. 2: Propose of the heuristic design

| Reward $r_n(\mathbf{p})$ | | The reward, denoted by $r_n(\mathbf{p})$, is defined as the average of total packet lengths of all the successful transmissions at state <i>n</i> . | | | |
|---------------------------------|--|---|--|--|--|
| | | | | | |
| | | (I) If $n \ge \gamma$, no reward is gained. (II) If $n < \gamma$ and $0 \le a \le \gamma - n$, the total packet lengths of these <i>a</i> new transmissions are regarded as the positive reward. | | | |

(III) If $n < \gamma$ and $\gamma - n < a \le N - n$, no positive reward is gained and the total packet lengths of the *n* ongoing transmissions in the carrier sensing phase are regarded as the negative reward.

$$\rightarrow r_n^{**}(\mathbf{p}) = \Lambda \sum_{a=0}^{\gamma-n} a \cdot \mu_{n,a}(\mathbf{p}_n) - 2n\Lambda \sum_{a=\gamma-n+1}^{N-n} \mu_{n,a}(\mathbf{p}_n)$$
$$\rightarrow R^{**}(\mathbf{p}) = \sum_{n=0}^{\gamma-1} \mu_n(\mathbf{p}) r_n^{**}(\mathbf{p})$$

 \rightarrow Satisfy the first condition of the policy iteration

Observation

Reward

 $r_{n}^{**}(\mathbf{p})$

When the system operates with **p** whose values are close to \mathbf{p}_{opt} , there is a small probability that a transmission suffers from severe conflict.

SevereIf a given transmission collides with new transmissions at more thanConflictone slot, we say this transmission suffers from severe conflict.

Mod. 2: Propose of the heuristic design

Optimization Problem

| Reward $r_n(\mathbf{p})$ | The reward lengths of a | , denoted by $r_n(\mathbf{p})$, is defined as the average of total packet all the successful transmissions at state n . | | | |
|--------------------------------------|---|--|--|--|--|
| Reward $r_n^{**}(\mathbf{p})$ | (I) If $n \ge \gamma$ (II) If $n < \gamma$ transmission (III) If $n < \gamma$ the total parameters $r_n^{**}(\mathbf{p}) =$ $\rightarrow R^{**}(\mathbf{p})$ \rightarrow Satisfy t | p, no reward is gained. p and $0 \le a \le \gamma - n$, the total packet lengths of these <i>a</i> new ns are regarded as the positive reward. p and $\gamma - n < a \le N - n$, no positive reward is gained and cket lengths of the <i>n</i> ongoing transmissions in the carrier ase are regarded as the negative reward. $= \Lambda \sum_{a=0}^{\gamma-n} a \cdot \mu_{n,a}(p_n) - 2n\Lambda \sum_{a=\gamma-n+1}^{N-n} \mu_{n,a}(p_n)$ $= \sum_{n=0}^{\gamma-1} \mu_n(\mathbf{p}) r_n^{**}(\mathbf{p})$ he first condition of the policy iteration | | | |
| | | | | | |
| Definition of The | | $\mathbf{p}_{heu} = \arg \max_{\mathbf{p} \in \mathbb{D}} R^{**}(\mathbf{p}), \ R_{heu} = \max_{\mathbf{p} \in \mathbb{D}} R(\mathbf{p}_{heu})$ | | | |

Mod. 2: Solve \mathbf{p}_{heu} by the policy iteration (Algorithm 2)

| 1. Initialization | n Choose an arbitrary parameter vector $\mathbf{p}^{(0)} \subset \mathbb{D}$ as the inivalue and set $k = 0$. | | | | |
|-------------------|---|--|--|--|--|
| 2. Evaluation | Calculate the relative value $v_n^*(\mathbf{p}^{(k)})$ for each $n \in S$ by Bellman equation. | | | | |
| 3. Improvement | For $n = 0, 1,, \gamma - 1$, update the new parameter as: $p_n^{(k+1)} = \arg \max_{p_n \in \mathbb{D}} r_n^{**}(p_n) + \sum_{n' \in S} \phi_{n,n'}(p_n) v_{n'}^{**}(\mathbf{p}^{(k)})$ | | | | |
| 4. Stopping Rule | If $\mathbf{p}^{(k+1)} = \mathbf{p}^{(k)}$, set $\mathbf{p}_{upp} = \mathbf{p}^{(k)}$ and stop. Otherwise, set $k = k + 1$ and go to step 2. | | | | |



Mod. 2: The iteration procedure of the parameters **p** and $R^*(\mathbf{p})$

Parameters: N=10, $\gamma=3$, $\Lambda=20$

Parameters: N=20, $\gamma=5$, $\Lambda=50$



Initialization: We set $p_0^{(k)} = \gamma/N$, and $p_n^{(k)} = 0$ for $1 \le n \le \gamma - 1$.

Conclusion: It can be seen that only **5 iterations** are needed to satisfy the stopping rule.

Mod 2: Comparisons between the heuristic design and *GlobalSearch* (*GS*)

The GS Solve (in *MATLAB Optimization Toolbox*) can be used to find global minima.

| N | Algorithm | Time | p 0 | <i>p</i> 1 | p ₂ | p 3 | p 4 | R |
|-----|------------------|----------------|------------|------------|-----------------------|------------|------------|--------|
| 10 | GS Solve | 4297.92s | 0.22079 | 0.16006 | 0.09995 | 0.04517 | 0.00699 | 3.5353 |
| | Heuristic Design | 18.77s | 0.22127 | 0.15934 | 0.09869 | 0.04402 | 0.00655 | 3.5348 |
| 10 | GS Solve | 2991.38s | 0.17681 | 0.12568 | 0.07676 | 0.03384 | 0.00509 | 3.5090 |
| 12 | Heuristic Design | 24.17s | 0.17711 | 0.12505 | 0.07574 | 0.03295 | 0.00476 | 3.5085 |
| 1.4 | GS Solve | 2886.17s | 0.14766 | 0.10358 | 0.06237 | 0.02708 | 0.00401 | 3.4928 |
| 14 | Heuristic Design | 30.28 s | 0.14786 | 0.10303 | 0.06152 | 0.02635 | 0.00374 | 3.4923 |
| 16 | GS Solve | 5758.00s | 0.12683 | 0.08814 | 0.05254 | 0.02257 | 0.00331 | 3.4818 |
| | Heuristic Design | 43.00 s | 0.12698 | 0.08765 | 0.05181 | 0.02196 | 0.00309 | 3.4813 |
| 10 | GS Solve | 19283.63s | 0.11120 | 0.07673 | 0.04540 | 0.01936 | 0.00281 | 3.4738 |
| 18 | Heuristic Design | 85.78s | 0.11131 | 0.07629 | 0.04476 | 0.01883 | 0.00263 | 3.4733 |
| 20 | GS Solve | 29465.91s | 0.09901 | 0.06795 | 0.03998 | 0.01694 | 0.00245 | 3.4678 |
| | Heuristic Design | 86.02s | 0.09910 | 0.06754 | 0.03941 | 0.01648 | 0.00228 | 3.4672 |

Conclusion: The near-optimal parameter vectors and throughtput solved in the heuristic design are basically the same as the optimal results solved by "GlobalSearch".

- Contrib. 3 Protocol Optimization
- Mod 2: Comparisons between the heuristic design and XL-CSMA

Remark: We set the maximum number of allowed retransmissions to be infinitely large.

XL-CSMA Each user adopts the access probabilities $p_n = \max(0, (\gamma^* - n) / (N - n))$ for $n = 0, 1, ..., \gamma - 1$, where the tuning parameter γ^* is an integer not larger than γ .



Conclusion: The heuristic design **significantly outperforms** optimal XL-CSMA in all the cases.

Mod 2: Convert the generalized *p*-persistent CSMA to a CSMA/CA

Remark: We set the maximum number of allowed retransmissions to 4.

Convert to CSMA/CA To convert the generalized *p*-persistent CSMA to a CSMA/CA scheme for IEEE 802.11-like networks, we require each user to maintain **contention window** *n* with the constant size $W_n = \lfloor 2/p_n - 1 \rfloor$ if $p_n > 0$ for n = 0, 1, ..., c - 1.

